

OptiTrust: an Interactive Optimization Framework

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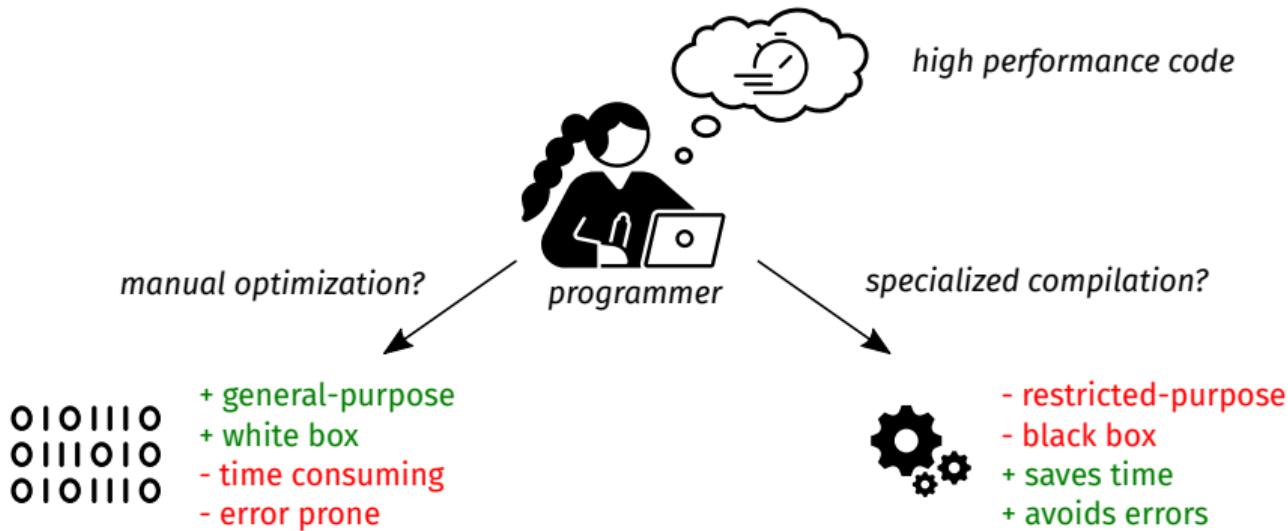
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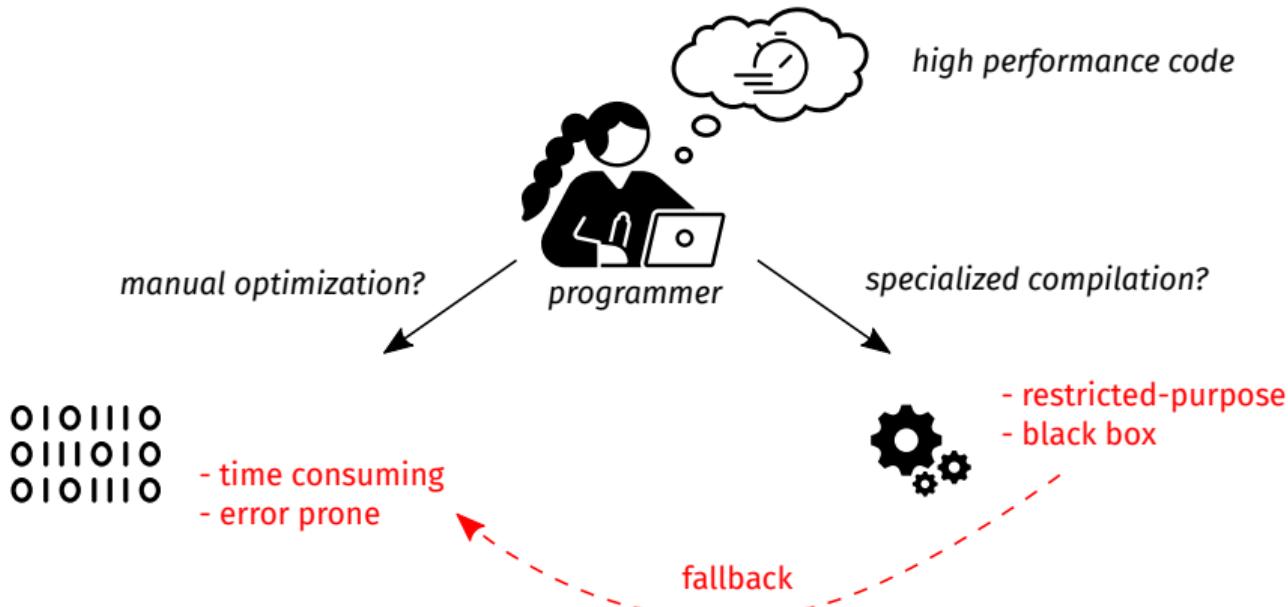


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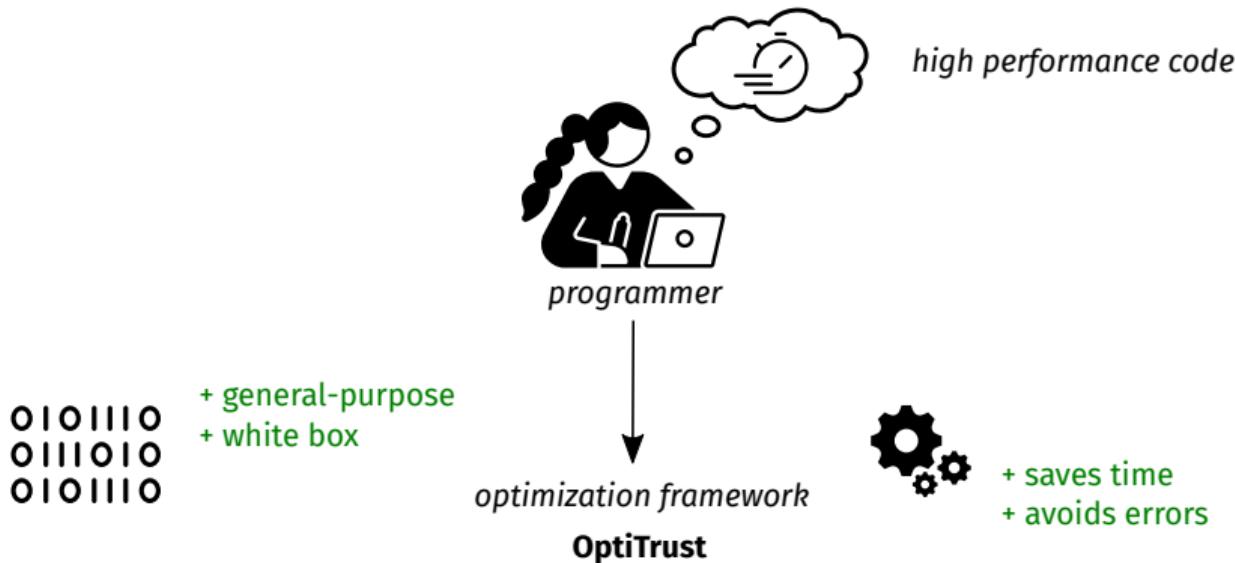
Why OptiTrust?



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Why OptiTrust?



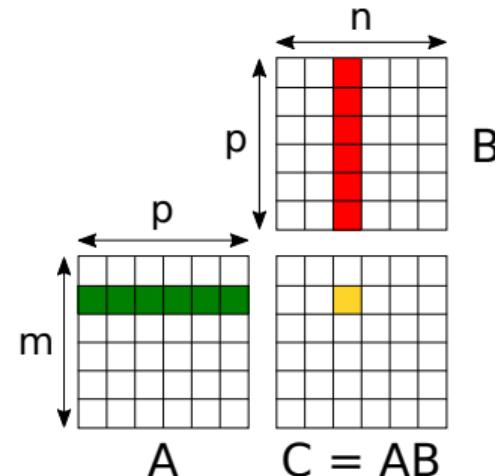
Example: Optimizing Matrix Multiplication

A standard benchmark to:

- ▶ showcase OptiTrust user experience
- ▶ compare to user-guided specialized compilers (*TVM*)

Unoptimized Matrix Multiplication

```
for (int i = 0; i < m; i++) {  
    for (int j = 0; j < n; j++) {  
        float sum = 0.0f;  
        for (int k = 0; k < p; k++) {  
            sum += A[i][k] * B[k][j];  
        }  
        C[i][j] = sum;  
    }  
}
```



Optimization by Hand

```
float* pB = (float*) malloc(sizeof(float[32][256][4][32]));
#pragma omp parallel for
for (int bj = 0; bj < 32; bj++) for (int bk = 0; bk < 256; bk++) {
    for (int k = 0; k < 4; k++) for (int j = 0; j < 32; j++) {
        pB[32768 * bj + 128 * bk + 32 * k + j] =
            B[1024 * (4 * bk + k) + 32 * bj + j]; }
}
#pragma omp parallel for
for (int bi = 0; bi < 32; bi++) for (int bj = 0; bj < 32; bj++) {
    float* sum = (float*) malloc(sizeof(float[32][32]));
    for (int i = 0; i < 32; i++) for (int j = 0; j < 32; j++) {
        sum[32 * i + j] = 0.; }
    for (int bk = 0; bk < 256; bk++) for (int i = 0; i < 32; i++) {
        float s[32];
        memcpy(s, &sum[32 * i], sizeof(float[32]));
    #pragma omp simd
        for (int j = 0; j < 32; j++) { // k = 0
            s[j] += A[1024 * (32 * bi + i) + 4 * bk + 0] *
                pB[32768 * bj + 128 * bk + 32 * 0 + j]; }
        // [...] k = 1, 2, 3
        memcpy(&sum[32 * i], s, sizeof(float[32])); }
    for (int i = 0; i < 32; i++) for (int j = 0; j < 32; j++) {
        C[1024 * (32*bi + i) + 32*bj + j] = sum[32*i + j]; }
}
// [...] free instructions
```

- ▶ Standard optimizations:
 - ▶ improve data locality
transform loops, change data layout
 - ▶ add parallelism
vectorization, multi-threading
- ▶ 150× faster
Intel i7-8665U, 4 cores, AVX2
- ▶ Time consuming
- ▶ Error prone
- ▶ 5× more lines of code

Optimization with TVM

TVM Algorithm = what to compute

```
k = tvm.reduce_axis((0, P))
A = tvm.placeholder((M, P))
B = tvm.placeholder((P, N))

C = tvm.compute((M, N),
    lambda i, j:
        sum(A[i, k] * B[k, j], axis=k))
```

Rewritten Algorithm

```
pB = tvm.compute((N / 32, P, 32),
    lambda bj, k, j:
        B[k, bj * 32 + j])

C = tvm.te.compute((M, N),
    lambda i, j:
        sum(A[i, k] *
            pB[j // 32, k, j % 32],
            axis=k))
```

TVM Schedule = how to compute

```
CC = s.cache_write(C, "global")
bi, bj, i, j = s[C].tile(
    C.op.axis[0], C.op.axis[1], 32, 32)
s[CC].compute_at(s[C], bj)
i2, j2 = s[CC].op.axis
(kaxis,) = s[CC].op.reduce_axis
bk, k = s[CC].split(kaxis, factor=4)
s[CC].reorder(bk, i2, k, j2)
s[CC].vectorize(j2)
s[CC].unroll(k)
s[C].parallel(bi)
bj3, _, j3 = s[pB].op.axis
s[pB].vectorize(j3)
s[pB].parallel(bj3)
```

- Convenient quickly try many schedules
- Restricted algorithm DSL + schedule API
- Black box implicit heuristics + unfamiliar IR

OptiTrust Transformation Script

OptiTrust Transformation Script

```
let tile (loop_id, size) = Loop.tile (int size) ~index:("b" ^ loop_id) ~bound:TileDivides [cFor loop_id] in
!! List.iter tile [("i", 32); ("j", 32); ("k", 4)];
!! Loop.reorder_at ~order:["bi"; "bj"; "bk"; "i"; "k"; "j"] [cPlusEq [cVar "sum"]];
!! Loop.hoist_expr ~dest:[tBefore; cFor "bi"] "pB" ~indep:["bi"; "i"] [cArrayRead "B"];
!! Function.inline_def [cFunDef "mm"];
!! Matrix.stack_copy ~var:"sum" ~copy_var:"s" ~copy_dims:1 [cFor ~body:[cPlusEq [cVar "sum"]] "k"];
!! Matrix.elim_mops [];
!! Loop.unroll [cFor ~body:[cPlusEq [cVar "s"]] "k"];
!! Omp.simd [nbMulti; cFor ~body:[cPlusEq [cVar "s"]] "j"];
!! Omp.parallel_for [nbMulti; cFunBody "mm1024"; cStrict; cFor ""];
```

- ▶ transformation script = sequence of transformation steps (!!)
- ▶ **transformation** = function modifying the current program
- ▶ *target* = data structure describing where to apply transformations
- ▶ scripts are written in OCaml: **let**, **List.iter**, ..

Interacting with OptiTrust

```
void mm(float* C, float* A, float* B, int m, int n, int p) {      void mm(float* C, float* A, float* B, int m, int n, int p) {  
-    for (int i = 0; i < m; i++) {  
-        for (int j = 0; j < n; j++) {  
-            float sum = 0.f;  
-  
-            for (int k = 0; k < p; k++) {  
-                sum += A[i][k] * B[k][j];  
-            }  
-            C[i][j] = sum;  
-        }  
-    }  
+    for (int bi = 0; bi < exact_div(m, 32); bi++) {  
+        for (int i = 0; i < 32; i++) {  
+            for (int bj = 0; bj < exact_div(n, 32); bj++) {  
+                for (int j = 0; j < 32; j++) {  
+                    float sum = 0.f;  
+                    for (int bk = 0; bk < exact_div(p, 4); bk++) {  
+                        for (int k = 0; k < 4; k++) {  
+                            sum += A[bi * 32 + i][bk * 4 + k] * B[bk * 4 + k][bj * 32 + j];  
+                        }  
+                    }  
+                    C[bi * 32 + i][bj * 32 + j] = sum;  
+                }  
+            }  
+        }  
+    }  
}
```

- ▶ pressing "F6" on a transformation step opens the corresponding diff. *first step above*
- ▶ pressing "Maj+F5" opens a trace of all transformations. *next slide*

!!! Loop.hoist_expr -dest:[tBefore; cFor "bi"] "pB" -indep:["bi"; "i"] [cArrayRead "B"];

- Variable.bind
- Loop.hoist_alloc
- Variable.init_detach
- Matrix.intro_malloc0
- Loop.hoist
- Loop.hoist
- Loop.move_out
- Instr.move
- Loop.hoist
- Loop.hoist
- Loop.move_out
- Instr.move
- Variable.to_const
- Variable.inline
- Variable.to_const
- Variable.inline
- Variable.to_const
- Variable.inline
- Variable.to_const
- Variable.rename
- Loop.hoist_insr
- Loop.fission
- Loop.fission
- Loop.move_out
- Loop.fission
- Instr.move
- Loop.fission
- Loop.move_out

```

1  #include "../../include/optitrust.h"
2  #include "matmul.h"
3  #include "omp.h"
4  // NOTE: using pretty matrix notation
5
6  void mm(float* C, float* A, float* B, int m, int n, int p) {
7
8      for (int bi = 0; bi < exact_div(m, 32); bi++) {
9          for (int bj = 0; bj < exact_div(n, 32); bj++) {
10             float* sum = (float*)malloc(sizeof(float[32][32]));
11             for (int i = 0; i < 32; i++) {
12                 for (int j = 0; j < 32; j++) {
13                     sum[i][j] = 0.f;
14                 }
15             }
16             for (int bk = 0; bk < exact_div(p, 4); bk++) {
17                 for (int i = 0; i < 32; i++) {
18                     for (int k = 0; k < 4; k++) {
19                         for (int j = 0; j < 32; j++) {
20                             sum[i][j] += A[bi * 32 + i][bk * 4 + k] * B[bk * 4 + k][bj * 32 + j];
21                         }
22                     }
23                 }
24             }
25             for (int i = 0; i < 32; i++) {
26                 for (int j = 0; j < 32; j++) {
27                     C[bi * 32 + i][bj * 32 + j] = sum[i][j];
28                 }
29             }
30             free(sum);
31         }
32     }
33 }
34 }
35 for (int i = 0; i < 32; i++) {
36     for (int j = 0; j < 32; j++) {
37         C[bi * 32 + i][bj * 32 + j] = sum[i][j];
38     }
39 }
40 free(sum);

```

!!! Loop.hoist_expr -dest:[tBefore; cFor "bi"] "pB" -indep:["bi"; "i"] [cArrayRead "B"];

- Variable.bind
- Loop.hoist_alloc
- Variable.init_detach
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- Variable.to_const
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- Variable.to_const
- Variable.inline
- Variable.to_const
- Variable.inline
- Variable.rename
- Loop.hoist_instr
- Loop.fission
- Loop.fission
- Loop.move_out
- Loop.fission
- Instr.move
- Loop.fission
- Loop.move_out

```

9     float* sum = (float*)malloc(sizeof(float[32][32]));
10    for (int i = 0; i < 32; i++) {
11        for (int j = 0; j < 32; j++) {
12            sum[i][j] = 0.f;
13        }
14    }
15    for (int bk = 0; bk < exact_div(p, 4); bk++) {
16        for (int i = 0; i < 32; i++) {
17            for (int k = 0; k < 4; k++) {
18                for (int j = 0; j < 32; j++) {
19                    sum[i][j] +=
20                     A[bi * 32 + i][bk * 4 + k] * B[bk * 4 + k][bj * 32 + j];
21                }
22            }
23        }
24    }
25    for (int i = 0; i < 32; i++) {
26        for (int j = 0; j < 32; j++) {
27            C[bi * 32 + i][bj * 32 + j] = sum[i][j];
28        }
29    }
30    free(sum);

```

```

9     float* sum = (float*)malloc(sizeof(float[32][32]));
10    for (int i = 0; i < 32; i++) {
11        for (int j = 0; j < 32; j++) {
12            sum[i][j] = 0.f;
13        }
14    }
15    for (int bk = 0; bk < exact_div(p, 4); bk++) {
16        for (int i = 0; i < 32; i++) {
17            for (int k = 0; k < 4; k++) {
18                for (int j = 0; j < 32; j++) {
19                    +   float pB = B[bk * 4 + k][bj * 32 + j];
20                    +   sum[i][j] += A[bi * 32 + i][bk * 4 + k] * pB;
21                }
22            }
23        }
24    }
25    for (int i = 0; i < 32; i++) {
26        for (int j = 0; j < 32; j++) {
27            C[bi * 32 + i][bj * 32 + j] = sum[i][j];
28        }
29    }
30    free(sum);

```

!!! Loop.hoist_expr -dest:[tBefore; cFor "bi"] "pB" -indep:["bi"; "i"] [cArrayRead "B"];

- Variable.bind
- **Loop.hoist_alloc**
- Variable.init_detach
- Matrix.intro_malloc0
- Loop.hoist
- Loop.hoist
- Loop.move_out
- Instr.move
- Loop.hoist
- Loop.hoist
- Loop.move_out
- Instr.move
- Variable.to_const
- Variable.inline
- Variable.to_const
- Variable.inline
- Variable.to_const
- Variable.inline
- Variable.inline
- Variable.rename
- Loop.hoist_insr
- Loop.fission
- Loop.fission
- Loop.move_out
- Loop.fission
- Loop.fission
- Loop.move_out

```

1  #include "../../include/optitrust.h"
2  #include "matmul.h"
3  #include "omp.h"
4  // NOTE: using pretty matrix notation
5
6  void mm(float* C, float* A, float* B, int m, int n, int p) {
7      for (int bi = 0; bi < exact_div(m, 32); bi++) {
8          for (int bj = 0; bj < exact_div(n, 32); bj++) {
9              float* sum = (float*)malloc(sizeof(float[32][32]));
10             for (int i = 0; i < 32; i++) {
11                 for (int j = 0; j < 32; j++) {
12                     sum[i][j] = 0.f;
13                 }
14             }
15             for (int bk = 0; bk < exact_div(p, 4); bk++) {
16                 for (int i = 0; i < 32; i++) {
17                     for (int k = 0; k < 4; k++) {
18                         for (int j = 0; j < 32; j++) {
19                             float pB = B[bk * 4 + k][bj * 32 + j];
20                             sum[i][j] += A[bi * 32 + i][bk * 4 + k] * pB;
21                         }
22                     }
23                 }
24             }
25             for (int i = 0; i < 32; i++) {
26                 for (int j = 0; j < 32; j++) {
27                     C[bi * 32 + i][bj * 32 + j] = sum[i][j];
28                 }
29             }
30             free(sum);
31         }
32     }
33 }
34
35 void mm1024(float* C, float* A, float* B) { mm(C, A, B, 1024, 1024, 1024); }
```

```

1  #include "../../include/optitrust.h"
2  #include "matmul.h"
3  #include "omp.h"
4  // NOTE: using pretty matrix notation
5
6  void mm(float* C, float* A, float* B, int m, int n, int p) {
7      + float* pB =
8      + (float*)malloc(sizeof(float[exact_div(n, 32)][exact_div(p, 4)][4][32]));
9      for (int bi = 0; bi < exact_div(m, 32); bi++) {
10         for (int bj = 0; bj < exact_div(n, 32); bj++) {
11             float* sum = (float*)malloc(sizeof(float[32][32]));
12             for (int i = 0; i < 32; i++) {
13                 for (int j = 0; j < 32; j++) {
14                     sum[i][j] = 0.f;
15                 }
16             }
17             for (int bk = 0; bk < exact_div(p, 4); bk++) {
18                 for (int i = 0; i < 32; i++) {
19                     for (int k = 0; k < 4; k++) {
20                         for (int j = 0; j < 32; j++) {
21                             + pB[bj][bk][k][j] = B[bk * 4 + k][bj * 32 + j];
22                             + sum[i][j] += A[bi * 32 + i][bk * 4 + k] * pB[bj][bk][k][j];
23                         }
24                     }
25                 }
26             }
27             for (int i = 0; i < 32; i++) {
28                 for (int j = 0; j < 32; j++) {
29                     C[bi * 32 + i][bj * 32 + j] = sum[i][j];
30                 }
31             }
32             free(sum);
33         }
34     }
35 + free(pB);
36 }
37
38 void mm1024(float* C, float* A, float* B) { mm(C, A, B, 1024, 1024, 1024); }
```

!!! Loop.hoist_expr -dest:[tBefore; cFor "bi"] "pB" -indep:["bi"; "i"] [cArrayRead "B"];

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```

1  #include "../../include/optitrust.h"
2  #include "matmul.h"
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4  // NOTE: using pretty matrix notation
5
6  void mm(float* C, float* A, float* B, int m, int n, int p) {
7      float* pB =
8          (float*)malloc(sizeof(float[exact_div(n, 32)][exact_div(p, 4)][4][32]));
9
10     for (int bi = 0; bi < exact_div(m, 32); bi++) {
11         for (int bj = 0; bj < exact_div(n, 32); bj++) {
12             float* sum = (float*)malloc(sizeof(float[32][32]));
13             for (int i = 0; i < 32; i++) {
14                 for (int j = 0; j < 32; j++) {
15                     sum[i][j] = 0.f;
16                 }
17             }
18             for (int bk = 0; bk < exact_div(p, 4); bk++) {
19                 for (int i = 0; i < 32; i++) {
20                     for (int k = 0; k < 4; k++) {
21                         for (int j = 0; j < 32; j++) {
22                             pB[bj][bk][k][j] = B[bk * 4 + k][bj * 32 + j];
23                             sum[i][j] += A[bi * 32 + i][bk * 4 + k] * pB[bj][bk][k][j];
24                         }
25                     }
26                 }
27                 for (int i = 0; i < 32; i++) {
28                     for (int j = 0; j < 32; j++) {
29                         C[bi * 32 + i][bj * 32 + j] = sum[i][j];
30                     }
31                 }
32             }
33         }
34     }
35     for (int i = 0; i < 32; i++) {
36         for (int j = 0; j < 32; j++) {
37             C[bi * 32 + i][bj * 32 + j] = sum[i][j];
38         }
39     }

```

Transformations are Composed into Abstractions

9 script steps result in >60 basic steps of >20 basic transformations:

- ▶ `Arith`: `simpl`
- ▶ `Sequence`: `delete`, `elim`
- ▶ `Function`: `inline`
- ▶ `Variable`: `inline`, `bind`, `init_detach`
- ▶ `Instr`: `move`
- ▶ `Array`: `inline_constant`
- ▶ `Matrix`: `intro_malloc0`, `copy_to_stack`, `elim_mindex`
- ▶ `Loop`: `fission`, `swap`, `hoist`, `move_out`, `tile`, `unroll`
- ▶ `Omp`: `parallel_for`, `simd`
- ▶ ...

Example Recap

OptiTrust Transformation Script

```
let tile (loop_id, size) = Loop.tile (* ... *) [cFor loop_id] in
  !! List.iter tile [("i", 32); ("j", 32); ("k", 4)];
  !! Loop.reorder_at -order:["bi"; "bj"; "bk"; "i"; "k"; "j"]
    [cPlusEq [cVar "sum"]];
  !! Loop.hoist_expr -dest:[tBefore; cFor "bi"] "pB"
    -indep:["bi"; "i"] [cArrayRead "B"];
  !! Function.inline_def [cFunDef "mm"];
  !! Matrix.stack_copy -var:"sum" -copy_var:"s" -copy_dims:1
    [cFor -body:[cPlusEq [cVar "sum"]] "k"];
  !! Matrix.elim_mops [];
  !! Loop.unroll [cFor -body:[cPlusEq [cVar "s"]] "k"];
  !! Omp.simd [nbMulti; cFor -body:[cPlusEq [cVar "s"]] "j"];
  !! Omp.parallel_for [nbMulti; cFunBody ""; cStrict; cFor ""];
```

TVM Schedule

```
CC = s.cache_write(C, "global")
bi, bj, i, j = s[C].tile(
  C.op.axis[0], C.op.axis[1], 32, 32)
s[CC].compute_at(s[C], bj)
i2, j2 = s[CC].op.axis
(kaxis,) = s[CC].op.reduce_axis
bk, k = s[CC].split(kaxis, factor=4)
s[CC].reorder(bk, i2, k, j2)
s[CC].vectorize(j2)
s[CC].unroll(k)
s[C].parallel(bi)
bj3, _, j3 = s[pB].op.axis
s[pB].vectorize(j3)
s[pB].parallel(bj3)
```

- achieves the same performance as the TVM schedule
- transforms C code rather than specialized languages / IRs
- is interactive, providing diffs and traces of familiar C code
- is reasonably concise compared to a specialized API

general-purpose

white box

still saves time

Ongoing Work: Justifying Transformation Correctness

- ▶ Memory resources are annotated in a subset of Separation Logic:

Initial Matrix Multiplication Annotations

```
void mm(float* C, float* A, float* B, int m, int n, int p) {  
    __modifies("C => Matrix(m, n)");  
    __reads("A => Matrix(m, p); B => Matrix(p, n)");  
    // [...]  
}
```

- ▶ From few annotations, resources are computed at every code location:

Computed Resources for Accumulation Instruction

```
__reads("A => Matrix(m, p); B => Matrix(p, n)");  
__modifies("sum => Cell");  
sum += A[i][k] * B[k][j];
```

Ongoing Work: Justifying Transformation Correctness

Transformations can:

- ▶ Leverage resources to justify their correctness: *avoids errors*

`Omp.parallel_for` is correct when each iteration has separate writes.

```
#pragma omp parallel for
for (int bi = 0; bi < exact_div(m, 32); bi++) {
    __only_this_iteration_modifies("C => MatrixTile ((bi, 32), (0, n))");
```

- ▶ Transform annotations to change view on resources:

`Omp.parallel_for ~modifies:"C => MatrixTile((bi, 32), (0, n))"`

```
--ghost("Matrix.tile_dim(C, (0, 32), (0, n))");
// ^ consumes 'C => Matrix(m, n)', produces C tiles
for (int bi = 0; bi < exact_div(m, 32); bi++) {
    __only_this_iteration_modifies("C => MatrixTile((bi, 32), (0, n))");
```

Conclusion

- ▶ OptiTrust is an interactive framework for optimizing general-purpose C code
- ▶ 3 existing case studies:
 - ▶ Matrix Multiplication : same performance as TVM in 9 script steps
 - ▶ Harris Corner Detection : same performance as Halide in 11 script steps ([Stencil.](#))
 - ▶ Particle-In-Cell : beyond specialized compilers in 140 script steps
- ▶ Questions for the ARRAY community:
 - ▶ Gradual transition between high-level array programming, and interactive optimization?
 - ▶ Implement array compilation techniques as transformations that can be reused and applied to hybrid code?

Conclusion

- ▶ OptiTrust is an interactive framework for optimizing general-purpose C code
- ▶ 3 existing case studies:
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- ▶ Questions for the ARRAY community:
 - ▶ Gradual transition between high-level array programming, and interactive optimization?
 - ▶ Implement array compilation techniques as transformations that can be reused and applied to hybrid code?



Thanks!

 optitrust.inria.fr

» [/traces/matmul.html](#)
» [/traces/harris.html](#)

Backup Slides

Matrix Multiplication Performance

- ▶ Intel(R) Core(TM) i7-8665U CPU, AVX2 (8 floats), 4 cores (8 hyperthreads)
- ▶ Relative speedup on 1024^3 input:

version	single-thread	multi-thread
unoptimized	1×	1×
optimized	46×	150×
TVM	46×	150×
numpy (Intel MKL) ¹	71×	183×

Both codes have 90th percentile runtime of 9.4ms over 200 benchmark runs, corresponding to a speedup of 150× compared to the 90th percentile of the naive code.

¹uses assembly code, explicit vectorization, custom thread library

Harris Script

OptiTrust transformation script for Harris corner detection

```
let fuse (ops, overlaps, outputs) =
  Stencil.fusion_targets ~nest_of:2 ~outputs ~overlaps [ctx; any cFun ops] in
let overlaps_2x2 vars = List.map (fun i -> i, [int 2; int 2]) vars in
!! List.iter fuse
[["grayscale"], [], ["gray"];
 ["sobelX"; "sobelY"], [], ["ix"; "iy"];
 ["mul"; "sum3x3"; "coarsity"], overlaps_2x2 ["ixx"; "ixy"; "iyy"], ["out"]];
!! Stencil.fusion_targets_tile [int 32] ~outputs:["out"]
~overlaps:["gray", [int 4]; "ix", [int 2]]
[ctx; nbMulti; cFor "y"];
!! simpl_mins [ctx];
!! Matrix.storage_folding ~dim:0 ~size:(int 4) [ctx; multi cVarDef ["gray"; "ix"; "iy"]];
!! Matrix.elim [ctx; multi cVarDef ["ixx"; "ixy"; "iyy"]];
let inline v = Matrix.inline_constant ~simpl ~decl:[cVarDef v] [ctx; nbMulti; cArrayRead v] in
!! List.iter inline ["weights_sobelX"; "weights_sobelY"; "weights_sum3x3"];
let bind_gradient name =
  Variable.bind_syntactic ~dest:[ctx; tBefore; cVarDef "acc_sxx"] ~fresh_name:(name ^ "${occ}") [ctx;
    cArrayRead name] in
!! List.iter bind_gradient ["ix"; "iy"];
!! Matrix.elim_mops [ctx];
!! Omp.parallel_for [ctx; cFor "y"];
!! Omp.simd ~clause:[Simdlen 8] [ctx; nbMulti; cFor "x"];
```

Expression Hoisting Transformation

`Loop.hoist_expr` is defined by combining simpler transformations.

```
let%transfo hoist_expr (* ... *) (tg : target) : unit =
  (* .. calls hoist_expr_loop_list .. *)
let%transfo hoist_expr_loop_list (* ... *) (tg : target) : unit =
  Target.iter (fun t p ->
    let instr_path = find_surrounding_instr p t in
    Variable.bind name (target_of_path p);
    hoist_decl_loop_list loops (target_of_path instr_path) tg)

let%transfo hoist_decl_loop_list (* ... *) (tg : target) : unit =
  (* .. calls hoist_alloc_loop_list .. *)
  (* .. calls hoist_instr_loop_list .. *)

let%transfo hoist_alloc_loop_list (* ... *) (tg : target) : unit =
  (* .. calls Variable.init_detach, Matrix.intro_malloc0, Instr.move,
     Loop.move_out, Loop.hoist .. *)

let%transfo hoist_instr_loop_list (* ... *) (tg : target) : unit =
  (* .. calls Instr.move, Loop.move_out, Loop.fission .. *)
```
